

Test 22 (Lessons 43–44): Logarithmic Functions and Their Applications

- 1) Paulo saved \$5500 from a summer job. He finds a high-yield savings account with 4.75% interest that compounds continuously. If Paulo does not add any more money to the account, how long will it take to save \$6000? $y = Pe^{rt}$

- 2) Write the inverse of $h(x)$.

$$h(x) = 8^{x-5}$$

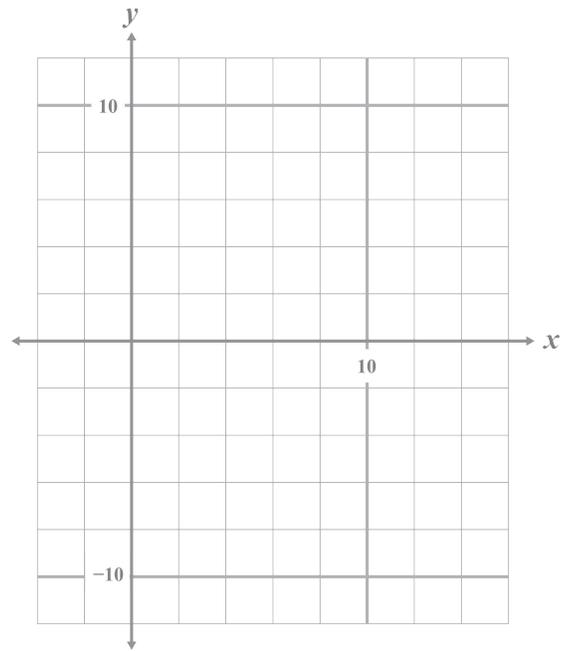
- 3) Name the domain and range of the inverse of $q(x)$.

$$q(x) = e^x + 3$$

- 4) Describe the transformation of the functions $f(x)$ to $g(x)$.

$$f(x) = \ln(x) + 5 \quad g(x) = \ln(x - 1)$$

- 5) Graph: $y = \log_2 x$



- 6) Name the end behavior of $y = \log_2 x$.

For problems 7–10 use the description below.

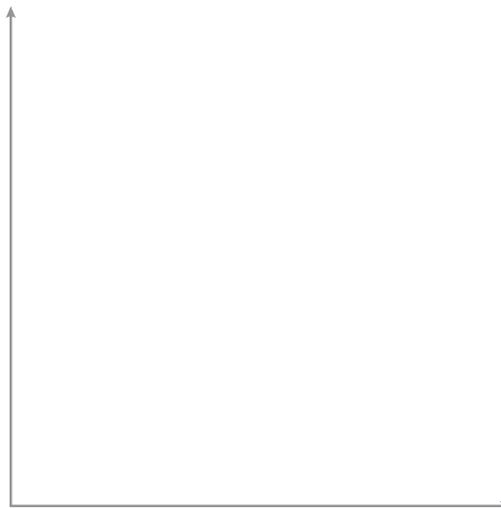
At 8:30 a.m., Douglas drinks a 16 ounce coffee containing 182 milligrams of caffeine. He knows the half-life of caffeine in regular coffee is about five hours. He found a formula that approximates the amount of caffeine in his system at any time:

$$C(t) = C_0 (0.5)^{\frac{t}{h}}$$

C_0 : Initial amount of caffeine
 t : Time in hours
 h : Half-life

7) Write the equation.

8) Sketch a graph. Include labels.



9) Determine the approximate amount of caffeine in Douglas' system at 8:30 a.m. the next day.

10) After how many hours will Douglas have one-fourth of the amount of caffeine that he started with that day?